

Physics School 2010: B Physics

Lecture 1: UT angles I (Belle/BaBar) Lecture 2: UT angles II (Belle/BaBar) Lecture 3: UT sides (Belle/BaBar/CDF/D0) Lecture 4: Future Super-b Factories

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Caveats:

- will not talk much about theoretical technical details
- will not discuss D0's new like-sign dilepton result
- will probably run out of time



A Unitarity triangle - determining the sides







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Variables: θ_{ℓ} , θ_{V} , χ , wwhere: $w = \frac{P_{B} \cdot P_{D^{*}}}{M_{B}M_{D^{*}}} = \frac{M_{B}^{2} + M_{D^{*}}^{2} - q^{2}}{2M_{B}M_{D^{*}}}$ and $q^{2} = (P_{\ell} + P_{\nu})^{2}$

Note: $q^2 = 0 \Rightarrow w = w_{max} = 1.50; w_{min} = 1 \quad q^2 = q^2_{max} = 10.69 \text{ GeV}^2$

 $\begin{array}{lll} \text{Decay rate:} & \frac{d^4\Gamma(B^0 \to D^{*-}\ell^+\nu_\ell)}{dw\,d(\cos\theta_\ell)\,d(\cos\theta_V)\,d\chi} &= \frac{6m_Bm_{D^*}^2}{8(4\pi)^4}\sqrt{w^2 - 1}(1 - 2wr + r^2)G_F^2|V_{cb}|^2 \ \times \\ & \left\{ (1 - \cos\theta_\ell)^2\sin^2\theta_V H_+^2(w) \ + \ (1 + \cos\theta_\ell)^2\sin^2\theta_V H_-^2(w) \\ & + 4\sin^2\theta_\ell\cos^2\theta_V H_0^2(w) \ - \ 2\sin^2\theta_\ell\sin^2\theta_V\cos2\chi H_+(w)H_-(w) \\ & - 4\sin\theta_\ell(1 - \cos\theta_\ell)\sin\theta_V\cos\varphi_V\cos\chi H_+(w)H_0(w) \\ & + 4\sin\theta_\ell(1 + \cos\theta_\ell)\sin\theta_V\cos\varphi_V\cos\chi H_-(w)H_0(w) \right\} \end{array}$

 V_{cb} via $B^0 \rightarrow D^{(*)} \ell \nu$

Differential decay rate:

b

d

$$\begin{array}{l} \displaystyle \frac{d^4 \Gamma(B^0 \to D^{*-}\ell^+ \nu_\ell)}{dw \, d(\cos \theta_\ell) \, d(\cos \theta_V) \, d\chi} &= \frac{6 m_B m_{D^*}^2}{8(4\pi)^4} \sqrt{w^2 - 1} (1 - 2wr + r^2) G_F^2 |V_{cb}|^2 \hspace{0.1cm} \times \\ & \left\{ (1 - \cos \theta_\ell)^2 \sin^2 \theta_V H_+^2(w) \hspace{0.1cm} + \hspace{0.1cm} (1 + \cos \theta_\ell)^2 \sin^2 \theta_V H_-^2(w) \right. \\ & \left. + 4 \sin^2 \theta_\ell \cos^2 \theta_V H_0^2(w) \hspace{0.1cm} - \hspace{0.1cm} 2 \sin^2 \theta_\ell \sin^2 \theta_V \cos 2\chi H_+(w) H_-(w) \right. \\ & \left. - 4 \sin \theta_\ell (1 - \cos \theta_\ell) \sin \theta_V \cos \theta_V \cos \chi H_+(w) H_0(w) \right. \\ & \left. + 4 \sin \theta_\ell (1 + \cos \theta_\ell) \sin \theta_V \cos \theta_V \cos \chi H_-(w) H_0(w) \right\} \end{array}$$

 $(H_+, H_-, H_0$ are helicity amplitudes)

Procedure to extract |V_{cb}|:

 Express helicity amplitudes in terms of functions h_{A1}(w), R₁(w), R₂(w) [these can be related to form factors A₁(w), A₂(w), A₃(w), V(w)]
 Parameterize these functions with analytic forms [e.g., Caprini et al., Nucl.Phys. B530, 153 (1998)]
 Integrate fully differential decay rate to get single differential distributions dΓ/dw, dΓ/dcosθ₁, dΓ/dcosθ_V, dΓ/dx that depend on h_{A1}(w), R₁(w), R₂(w)
 Fit data for *F*(w)|V_{cb}|, extrapolate back to w=1
 Use theory to calculate *F*(1), determine |V_{cb}|

 V_{cb} via $B^0 \rightarrow D^{(*)} \ell \nu$



Procedure to extract |V_{cb}|:
1) Express helicity amplitudes in terms of functions h_{A1}(w), R₁(w), R₂(w) [these can be related to form factors A₁(w), A₂(w), A₃(w), V(w)]
2) Parameterize these functions with analytic forms [e.g., Caprini et al., Nucl.Phys. B530, 153 (1998)]
3) Integrate fully differential decay rate to get single differential distributions dΓ/dw, dΓ/dcosθ₁, dΓ/dcosθ_V, dΓ/dx that depend on h_{A1}(w), R₁(w), R₂(w)
4) Fit data for *F*(w)|V_{cb}|, extrapolate back to w=1
5) Use theory to calculate *F*(1), determine |V_{cb}|

$$egin{aligned} H_{\pm}(w) &= M_B rac{R^*(r+1)(w+1)}{2} \, h_{A_1}(w) \left[1 \mp \sqrt{rac{w-1}{w+1}} R_1(w)
ight] \ H_0(w) &= M_B rac{R^*(1-r^2)(w+1)}{2\sqrt{1-2wr+r^2}} \, h_{A_1}(w) \left[1 + rac{(w-1)(1-R_2(w))}{1-r}
ight] \ egin{aligned} R^* &= rac{2\sqrt{M_B M_{D^*}}}{M_B + M_{D^*}} \ rac{h_{A_1}(w) &= h_{A_1}(1) \left[1 - 8
ho^2 z + (53
ho^2 - 15) z^2 - (231
ho^2 - 91) z^3
ight] \ egin{aligned} (w) &= \sqrt{w+1} - \sqrt{2} \ rac{\sqrt{w+1} - \sqrt{2}}{2} \ rac{1}{2} \, rac{1}{$$

$$egin{array}{rll} R_1(w) &= & R_1(1) - 0.12(w-1) + 0.05(w-1)^2 \ R_2(w) &= & R_2(1) + 0.11(w-1) - 0.06(w-1)^2 \end{array}$$

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 $z = \frac{1}{\sqrt{w+1} + \sqrt{2}}$

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 V_{ch} via $B^0 \rightarrow D^{(*)} \ell v$



Procedure to extract $|V_{cb}|$: _____

 Express helicity amplitudes in terms of functions h_{A1}(w), R₁(w), R₂(w) [these can be related to form factors A₁(w), A₂(w), A₃(w), V(w)]
 Parameterize these functions with analytic forms [e.g., Caprini et al., Nucl.Phys. B530, 153 (1998)]
 Integrate fully differential decay rate to get single differential distributions dΓ/dw, dΓ/dcosθ₁, dΓ/dcosθ_V, dΓ/dx that depend on h_{A1}(w), R₁(w), R₂(w)

4) Fit data for $\mathcal{F}(w)|V_{cb}|$, extrapolate back to w=1

5) Use theory to calculate $\mathcal{F}(1)$, determine $|V_{cb}|$

$$\begin{split} \left| \frac{d\Gamma}{dw} &= \frac{G_F^2}{48\pi^3} M_{D^*}^3 (M_B - m_{D^*})^2 |V_{cb}|^2 \times \\ &\sqrt{w^2 - 1} (w+1)^2 \left[1 + \frac{4w}{w+1} \left(\frac{1 - 2wr + r^2}{(1 - r)^2} \right) \right] \ \mathcal{F}^2(w) \\ & \left\{ 2 \frac{1 - 2wr + r^2}{(1 - r)^2} \left[1 + \frac{w - 1}{w+1} R_1^2(w) \right] + \left[1 + \frac{w - 1}{1 - r} \left(1 - R_2(w) \right) \right]^2 \right\} \frac{R^{*2}(w+1)^2}{4} h_{a_1}^2(w) \end{split}$$



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Adachi et al. (Belle), arXiv:0810.1657 [140 fb⁻¹, 69k signal cand.]



$$egin{array}{rll} egin{array}{lll} R_1(1) &=& 1.200 \pm 0.040 \pm 0.020 \ R_1(1) &=& 1.495 \pm 0.050 \pm 0.062 \ R_2(1) &=& 0.844 \pm 0.034 \pm 0.019 \ \mathcal{F}(1) |V_{cb}| &=& (34.4 \pm 0.2 \pm 1.0) imes 10^{-3} \end{array}$$



-laviA V_{cb} via Global Fit to Moments

Schwanda et al. (Belle), PRD 78, 032016 (2008) http://www.slac.stanford.edu/xorg/hfag/semi/fpcp2009/gbl_fits/kinetic/index.html

Operator product expansion (OPE) and Heavy Quark Effective theory (HQET) predict various moments of distributions as a function of $|V_{cb}|$, mb, and several non-perturbative HQ parameters \Rightarrow fit the data for all these parameters, obtain $|V_{cb}|$

"1S Scheme" [Bauer et al., PRD 70, 094017 (2004)] (can also use the "Kinetic Scheme," Gambino et al., EPJ C34, 181 (2004); Benson et al., Nucl. Phys. B710, 371 (2005)

Partial branching fraction:

$$\Delta {\cal B}_{E_{
m min}} \ = \ rac{G_F^2\,m^5}{192\pi^3} \, |V_{cb}|^2 \, \eta_{
m QED} au_B \left\langle X
ight
angle_{\Delta {\cal B}, E_{
m min}}$$

where:

$$\begin{split} \langle X \rangle_{E_{min}} \; = \; X^{(1)} + X^{(2)} \Lambda + X^{(3)} \Lambda^2 + X^{(4)} \Lambda^3 + \\ & X^{(5)} \lambda_1 + X^{(6)} \Lambda \lambda_1 + X^{(7)} \lambda_2 + X^{(8)} \Lambda \lambda_1 + \\ & X^{(9)} \rho + X^{(10)} \rho_2 + X^{(11)} \tau_1 + X^{(12)} \tau_2 + X^{(13)} \tau_3 + X^{(14)} \tau_4 + \\ & X^{(15)} \epsilon + X^{(16)} \epsilon_{\text{BLM}}^2 + X^{(17)} \Lambda \epsilon \end{split}$$

 $X^{(i)}$ are perturbatively calculated coefficients; HQ parameters are Λ (leading order), λ_1 , λ_2 (order $1/m_b^2$), ρ_1 , ρ_2 , τ_1 , τ_2 , τ_3 , τ_4 (order $1/m_b^3$).

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V_{cb} via Global Fit to Moments

| Analysis | Moments <(E- <e>)ⁿ></e> |
|----------------------------|--|
| $B \to X_c \ell v$ | E_{ℓ}, M_{χ}^2 |
| $B \rightarrow X_s \gamma$ | E_{γ} |

| BaBar | n=2 c=0.9,1.1,1.3,1.5 n=4 c=0.9,1.0,1.2,1.4 [1] | n=0 c=0.6,1.2,1.5 n=1 c=0.6,0.8,1.0,1.2,1.5 n=2 c=0.6,1.0,1.5 n=3 c=0.8,1.2 [2] | n=1 c=1.9,2.0 n=2 c=1.9 [3,4] | [1] Phys.Rev. D69 (2004) 111103 [2] Phys.Rev. D69 (2004) 111104 [3] Phys.Rev. D72 (2005) 052004 [4] Phys. Rev. Lett. 97, 171803 (2006) |
|--------|---|--|------------------------------------|---|
| Belle | n=2 c=0.7,1.1,1.3,1.5 n=4 c=0.7,0.9,1.3 [5] | n=0 c=0.6,1.0,1.4 n=1 c=0.6,0.8,1.0,1.2,1.4 n=2 c=0.6,1.0,1.4 n=3 c=0.8,1.0, 1.2 [6] | n=1 c=1.8,1.9 n=2 c=1.8,2.0 [7] | [5] Phys.Rev. D75 (2007) 032005 [6] Phys.Rev. D75 (2007) 032001 [7] Phys.Rev. D78 (2008) 032016 |
| CDF | n=2 c=0.7 n=4 c=0.7 [8] | | | [8] Phys.Rev. D71 (2005) 051103 |
| CLEO | n=2 c=1.0,1.5 n=4 c=1.0,1.5 [9] | | n=1 c=2.0 [10] | [9] Phys.Rev. D70 (2004) 032002 [10] Phys.Rev.Lett. 87 (2001) 251807 |
| DELPHI | n=2 c=0.0 n=4 c=0.0 [11] | n=1 c=0.0 n=2 c=0.0 n=3 c=0.0 [11] | | [11] Eur.Phys.J. C45 (2006) 35-59 |

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het A V_{cb} via Global Fit to Moments



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"Kinetic Scheme"

Gambino et al., EPJ C34, 181 (2004); Benson et al., Nucl. Phys. B710, 371 (2005) http://www.slac.stanford.edu/xorg/hfag/semi/fpcp2009/gbl_fits/kinetic/index.html







 $\Gamma(\pi \ell v)$ proportional to $|V_{ub}|^2 x$ (form factor)²

 \Rightarrow need calculation of form factor to extract $|V_{ub}|$

Two strategies:

light cone sum rules (low q², high hadron momentum) lattice calculation (high q², low hadron momentum)

The labels " B_{reco} " and "SL" tags refer to the type of B decay tag used.

| | $\mathcal{B}[10^{-4}]$ | $\mathcal{B}(q^2 > 16 \ \mathrm{GeV}^2/c^2)[10^{-4}]$ | $\mathcal{B}(q^2 < 16 \text{ GeV}^2/c^2)[10^{-4}]$ |
|------------------------|--------------------------|---|--|
| CLEO π^+, π^0 | $1.38 \pm 0.15 \pm 0.11$ | $0.41 \pm 0.08 \pm 0.04$ | $0.97 \pm 0.13 \pm 0.09$ |
| BABAR π^+ | $1.45 \pm 0.07 \pm 0.11$ | $0.38 \pm 0.04 \pm 0.05$ | $1.08 \pm 0.06 \pm 0.09$ |
| BELLE SL π^+ | $1.38 \pm 0.19 \pm 0.15$ | $0.36 \pm 0.10 \pm 0.04$ | $1.02 \pm 0.16 \pm 0.11$ |
| BELLE SL π^0 | $1.43 \pm 0.26 \pm 0.15$ | $0.37 \pm 0.15 \pm 0.04$ | $1.05 \pm 0.23 \pm 0.11$ |
| BABAR SL π^+ | $1.39 \pm 0.21 \pm 0.08$ | $0.46 \pm 0.13 \pm 0.03$ | $0.92 \pm 0.16 \pm 0.05$ |
| BABAR SL π^0 | $1.80 \pm 0.28 \pm 0.15$ | $0.45 \pm 0.17 \pm 0.06$ | $1.38 \pm 0.23 \pm 0.11$ |
| BABAR $B_{reco} \pi^+$ | $1.07 \pm 0.27 \pm 0.19$ | $0.65 \pm 0.20 \pm 0.13$ | $0.42 \pm 0.18 \pm 0.06$ |
| BABAR $B_{reco} \pi^0$ | $1.54 \pm 0.41 \pm 0.30$ | $0.49 \pm 0.23 \pm 0.12$ | $1.05 \pm 0.36 \pm 0.19$ |
| BELLE $B_{reco} \pi^+$ | $1.12 \pm 0.18 \pm 0.05$ | $0.26 \pm 0.08 \pm 0.01$ | $0.85 \pm 0.16 \pm 0.04$ |
| BELLE $B_{reco} \pi^0$ | $1.24 \pm 0.23 \pm 0.05$ | $0.41 \pm 0.11 \pm 0.02$ | $0.85 \pm 0.16 \pm 0.04$ |
| Average | $1.36 \pm 0.05 \pm 0.05$ | $0.37 \pm 0.02 \pm 0.02$ | $0.94 \pm 0.05 \pm 0.04$ |

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Using the average results from previous slide:

The first uncertainty is experimental, and the second is from theory.

| Method | $V_{ub}[10^{-3}]$ |
|-------------------------------------|---------------------------------|
| LCSR, full q^2 | $3.45 \pm 0.11^{+0.67}_{-0.42}$ |
| $LCSR, q^2 < 16 \text{ GeV}^2/c^2$ | $3.34 \pm 0.12^{+0.55}_{-0.37}$ |
| HPQCD, full q^2 | $3.05 \pm 0.10^{+0.73}_{-0.43}$ |
| HPQCD, $q^2 > 16 \text{ GeV}^2/c^2$ | $3.40 \pm 0.20^{+0.59}_{-0.39}$ |
| FNAL, full q^2 | $3.73 \pm 0.12^{+0.88}_{-0.52}$ |
| FNAL, $q^2 > 16 \text{ GeV}^2/c^2$ | $3.62 \pm 0.22^{+0.63}_{-0.41}$ |
| APE, full q^2 | $3.59 \pm 0.11^{+1.11}_{-0.57}$ |
| APE, $q^2 > 16 \text{ GeV}^2/c^2$ | $3.72 \pm 0.21^{+1.43}_{-0.66}$ |

(for references see HFAG semileptonic web page: http://www.slac.stanford.edu/xorg/hfag/semi/index.html)

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 V_{ub} via $B^0 \rightarrow X_u \ell^+ \nu$

This is very challenging due to huge background from $B^0 \rightarrow X_c \ell^+ \nu$ decays. To isolate signal, cuts are required that substantially reduce the acceptance. To calculate the partial rates for these restricted kinematic regions is complicated and requires much theoretical machinery. HFAG considers 5 theoretical frameworks:

> Lange et al. (BLNP), PRD 72, 073006 (2005) Andersen, Gardi (DGE), JHEP 601, 97 (2006) Gambino et al. (GGOU), JHEP 710, 58 (2007) Aglietti et al. (ADFR), EPJ C59 (2009); Nucl. Phy. B768, 85 (2007) Bauer et al. (BLL), PRD64, 113004 (2001)

The Data:

| Measurement | Accepted region | $\Delta \mathcal{B}[10^{-4}]$ | Notes |
|------------------|---|-------------------------------|----------------------------|
| CLEO [1] | $E_e > 2.1 \mathrm{GeV}$ | $3.3 \pm 0.2 \pm 0.7$ | |
| BaBar [2] | $E_e > 2.0 \mathrm{GeV}, s_{\mathrm{h}}^{\mathrm{max}} < 3.5 \mathrm{GeV}^2$ | $4.4\pm0.4\pm0.4$ | |
| BaBar [3] | $E_e > 2.0 \mathrm{GeV}$ | $5.7\pm0.4\pm0.5$ | |
| BELLE [4] | $E_e > 1.9 \mathrm{GeV}$ | $8.5\pm0.4\pm1.5$ | |
| BaBar [5] | $M_X < 1.7 \ { m GeV}/c^2, q^2 > 8 \ { m GeV}^2/c^2$ | $7.7\pm0.7\pm0.7$ | 65% correlation with BaBar |
| | | | M_X analysis |
| BELLE [6] | $M_X < 1.7 \ { m GeV}/c^2, q^2 > 8 \ { m GeV}^2/c^2$ | $7.4 \pm 0.9 \pm 1.3$ | |
| BaBar [5] | $P_+ < 0.66 \mathrm{GeV}$ | $9.4\pm0.9\pm0.8$ | 38% correlation with BaBar |
| | | | $(M_X - q^2)$ analysis |
| BaBar [5] | $M_X < 1.55 \mathrm{GeV}/c^2$ | $11.7 \pm 0.9 \pm 0.7$ | 67% correlation with BaBar |
| | | | P_+ analysis |
| BELLE [7] | $p_\ell^* > 1 \text{ GeV}/c$ | $19.6 \pm 1.7 \pm 1.6$ | |

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 V_{ub} via $B^0 \rightarrow X_u \ell^+ \nu$

Data vs. Theoretical scheme (references correspond to previous slide): (see also http://www.slac.stanford.edu/xorg/hfag/semi/index.html)

The errors quoted are experimental and theoretical, respectively.

| | BLNP | DGE | GGOU | ADFR | BLL |
|----------------------------------|--------------------------------------|---------------------------------|---------------------------------|---------------------------------|---------------------------------|
| Input parameters | | | | | |
| scheme | SF | \overline{MS} | kinetic | \overline{MS} | 1S |
| $m_b \; ({\rm GeV})$ | $4.620 \ ^{+0.039}_{-0.032}$ | 4.222 ± 0.051 | 4.591 ± 0.031 | 4.222 ± 0.051 | 4.70 ± 0.03 |
| $\mu_{\pi}^2 \; (\text{GeV}^2)$ | $0.288 \stackrel{+0.054}{_{-0.074}}$ | <u> </u> | 0.454 ± 0.038 | - | - |
| Ref. | | | $ V_{ub} $ values | | |
| E_e [1] | $4.01 \pm 0.47^{+0.34}_{-0.34}$ | $3.71 \pm 0.43^{+0.30}_{-0.26}$ | $3.82 \pm 0.45^{+0.22}_{-0.39}$ | $3.47 \pm 0.41^{+0.21}_{-0.22}$ | - |
| M_X, q^2 [6] | $4.40 \pm 0.46^{+0.31}_{-0.19}$ | $4.31 \pm 0.45^{+0.24}_{-0.23}$ | $4.25 \pm 0.45^{+0.25}_{-0.33}$ | $3.94 \pm 0.41^{+0.23}_{-0.24}$ | $4.67 \pm 0.49^{+0.34}_{-0.34}$ |
| E_e [4] | $4.82 \pm 0.45^{+0.32}_{-0.29}$ | $4.67 \pm 0.43^{+0.26}_{-0.25}$ | $4.66 \pm 0.43^{+0.19}_{-0.30}$ | $4.53 \pm 0.42^{+0.27}_{-0.27}$ | - |
| E_e [3] | $4.36 \pm 0.25^{+0.31}_{-0.30}$ | $4.16 \pm 0.28^{+0.28}_{-0.25}$ | $4.18 \pm 0.24^{+0.20}_{-0.33}$ | $3.98 \pm 0.27^{+0.24}_{-0.25}$ | - |
| E_{e}, s_{h}^{\max} [2] | $4.49 \pm 0.30^{+0.39}_{-0.37}$ | $4.16 \pm 0.28^{+0.30}_{-0.30}$ | - | $3.87 \pm 0.26^{+0.24}_{-0.24}$ | |
| p_{ℓ}^{*} [7] | $4.46 \pm 0.27^{+0.24}_{-0.21}$ | $4.54 \pm 0.27^{+0.15}_{-0.15}$ | $4.48 \pm 0.27^{+0.11}_{-0.15}$ | $4.55 \pm 0.30^{+0.27}_{-0.27}$ | - |
| M_X [5] | $4.20 \pm 0.20^{+0.29}_{-0.27}$ | $4.41 \pm 0.21^{+0.23}_{-0.20}$ | $4.12 \pm 0.20^{+0.25}_{-0.28}$ | $4.01 \pm 0.19^{+0.25}_{-0.26}$ | - |
| M_X, q^2 [5] | $4.49 \pm 0.29^{+0.32}_{-0.29}$ | $4.37 \pm 0.29^{+0.24}_{-0.23}$ | $4.34 \pm 0.28^{+0.26}_{-0.34}$ | $4.12 \pm 0.26^{+0.24}_{-0.25}$ | $4.88 \pm 0.32^{+0.36}_{-0.36}$ |
| <i>P</i> ₊ [5] | $3.83 \pm 0.25^{+0.27}_{-0.25}$ | $3.86 \pm 0.25^{+0.35}_{-0.28}$ | $3.57 \pm 0.23^{+0.28}_{-0.27}$ | $3.53 \pm 0.23^{+0.23}_{-0.23}$ | - |
| M_X, q^2 [8] | - | - | - | - | $4.97 \pm 0.39^{+0.37}_{-0.37}$ |
| Average | $4.32 \pm 0.16^{+0.22}_{-0.23}$ | $4.46 \pm 0.16^{+0.18}_{-0.17}$ | $4.34 \pm 0.16^{+0.15}_{-0.22}$ | $4.16 \pm 0.14^{+0.25}_{-0.22}$ | $4.87 \pm 0.24^{+0.38}_{-0.38}$ |

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Adachi et al., arXiv:0809.3834; Ikado et al., PRL 97 251802 (1996)

$$\mathcal{B}(B^+ \to \tau^+ \nu_\tau) = \frac{G_F^2 m_B}{8\pi} m_\tau^2 \left(1 - \frac{m_\tau^2}{m_B^2}\right)^2 f_B^2 |V_{ub}|^2 \tau_B$$

Semileptonic tag:

 $B^+ \rightarrow D^{(*)0}\ell^+\nu, D^{*0} \rightarrow D^0\gamma, D^0\pi^0 \quad D^0 \rightarrow K\pi, K\pi\pi^0, K\pi\pi\pi$ $\tau \rightarrow \mu\nu\nu, e\nu\nu, \pi\nu$ (1 charged track) in signal hemisphere

•Dominant backgrounds are $b \rightarrow c$ (BB) and continuum

Signal is obtained by fitting the ECL (electromagnetic calorimeter energy) distribution: peak new zero indicates $\tau \rightarrow \ell \nu \nu, \pi \nu$ decay.

■ ECL simulation is validated with identically tagged $B^+ \rightarrow D^{(*)0} \ell^+ v$ control sample

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rst evidence. 3.5 σ





Adachi et al., arXiv:0809.3834; Ikado et al., PRL 97 251802 (1996)

$$\begin{array}{lll} \mathcal{B}(B^+ \to \tau^+ \nu) &=& \left(1.65 \, {}^{+0.38}_{-0.37} \, {}^{+0.35}_{-0.37}\right) \times 10^{-4} \\ \Rightarrow & f_B |V_{ub}| &=& 0.97 \, \pm 0.11 \, {}^{+0.10}_{-0.11} & \mathrm{MeV} \\ \Rightarrow & |V_{ub}| &=& \left[0.51 \, \pm 0.08 \, (\mathrm{exp.}) \, \pm 0.06 \, (\mathrm{theor.})\right] \% \end{array}$$

World average:

 $\mathcal{B}(B^+ \rightarrow \tau^+ \nu) = (1.67 \pm 0.39) \times 10^{-4}$ 2.4 σ discrepancy with the value predicted by the CKM fit:

Tension is coming from $|V_{td}|$ measured in $B^0-\overline{B}^0$ mixing, $\phi_1(\beta)$ and $\phi_2(\alpha)$:



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PRL 101, 111801 (2008) [605 fb⁻¹] b d s V_{td}* V_{ts}* V_{tb} W

Combined fit assuming

$$\begin{split} \mathcal{B}_{\rho^+\gamma} &= 2\left(\frac{\tau_{B^+}}{\tau_{B^0}}\right) \mathcal{B}_{\rho^0\gamma} = 2\left(\frac{\tau_{B^+}}{\tau_{B^0}}\right) \mathcal{B}_{\omega\gamma}\\ gives\\ \mathcal{B}(B \rightarrow \rho\gamma) &= (1.14 \pm 0.20 \ ^{+0.10} \ _{-0.12})\\ & \times 10^{-6} \end{split}$$

Taking ratio to
$$\mathcal{B}(B \rightarrow K^*\gamma)$$
 gives
| V_{td}/V_{ts} | = 0.195 ^{+0.020} -0.019 ± 0.01

Ball et al., PRD 75, 054004 (2007) Ali et al., PLB 595, 323 (2004)





Most precise value of $|V_{td}/V_{ts}|$ is obtained from measurements of B_s - B_s mixing made by CDF.

Abulencia et al. (CDF), PRL 97, 242003 (2006) [1 fb⁻¹]

$$b \frac{V_{tb}^{*} V_{ts}}{U,C,t} s \qquad \Delta m_{s} = \frac{G_{F}^{2} M_{W}^{2}}{6\pi^{2}} |V_{ts}^{*} V_{tb}|^{2} \eta_{QCD} S_{0}(x_{t}) M_{B_{s}} f_{B_{s}}^{2} \hat{B}_{B_{s}}}{\bar{s} u,\bar{c},\bar{t}} \bar{b} \qquad \left(\Delta m_{d} = \frac{G_{F}^{2} M_{W}^{2}}{6\pi^{2}} |V_{td}^{*} V_{tb}|^{2} \eta_{QCD} S_{0}(x_{t}) M_{B_{d}} f_{B_{d}}^{2} \hat{B}_{B_{d}}}\right)$$

But many differences between hadronic experimental measurements and e⁺e⁻ measurements:

many more B's produced, but only a tiny fraction triggered on and reconstructed

- much higher background
- much poorer π/K discrimination
- much poorer flavor tagging

kinematic function constant



Dalgic et al. (HPQCD), PRD 76, 011501 (2007)



Abulencia et al. (CDF), PRL 97, 242003 (2006) [1 fb⁻¹]



$$\mathbf{F}_{net} \mathbf{A} \quad V_{ts} \text{ via } B_s - \overline{B}_s \text{ mixing (CDF)}$$

Abulencia et al. (CDF), PRL 97, 242003 (2006) [1 fb⁻¹]

Three methods to measure mixing: amplitude scan, likelihood scan, likelihood fit



From likelihood fit: $\Delta m = (17.77 \pm 0.10 \pm 0.07) \text{ ps}^{-1}$

 $\Rightarrow \quad \left| \frac{V_{td}}{V_{ts}} \right| \; = \; \xi \sqrt{\frac{\Delta m_d \, m_{B_s}}{\Delta m_s \, m_{B^0}}} \; = \; 0.2060 \, \pm 0.0007 \, (\text{exp.}) \, {}^{+0.0081}_{-0.0060} (\text{theor.})$

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Abulencia et al. (CDF), PRL 100, 161802 (2008) [1.3 fb⁻¹] CDF Public Note 9458 (2009) [2.8 fb⁻¹] CDF Public Note 9787 (2009) [2.8 fb⁻¹ (CDF) + 2.8 fb⁻¹ (D0)]

METHOD:

Select $B^0 \rightarrow J/\psi \phi$ decays. This state can decay to both CP-even and CP-odd eigenstates – it depends on L (orbital angular momentum of J/ψ , ϕ pair). If you could separate the final states into these two categories, and measure the lifetime (1/ Γ) for each category, you would determine $\Delta\Gamma$. But one <u>CAN</u> do this statistically (i.e., not event-by-event): do an unbinned ML fit to the angular distribution (to determine the CP) and decay time (to determine $1/\Gamma$ and $\Delta\Gamma$). Finally: add flavor-tagging information (a probability density function) into the likelihood function; this allows one to also fit for the CPV parameter $\beta_{\rm s} = \operatorname{Arg}[-V_{tb}V_{ts}/(V_{cb}V_{cs})].$

Fit parameters:

$$egin{aligned} eta_s, & \Delta\Gamma_s = \Gamma_1 - \Gamma_2, & \Gamma = (\Gamma_1 + \Gamma_2)/2 = 1/ au, & \Delta m_s, \ f_s, & \left|A_0
ight|^2, & \left|A_{\perp}
ight|^2, & \left|A_{\parallel}
ight|^2, \ \delta_{\parallel} = \mathrm{Arg}[A_{\parallel}^*A_0], & \delta_{\perp} = \mathrm{Arg}[A_{\perp}^*A_0] \end{aligned}$$

Fit variables:





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$\begin{array}{c} Flavi \\ \hline net \end{array} A \quad CDF \ measurement \ of \ \Delta \Gamma_s, \ \beta_s \end{array}$

Probability density function (PDF) for angles, decay time:

$$egin{aligned} P(t, heta_T,\psi_T,\phi_T) &= ig|A_0ig|^2 \ 2\cos^2\psi_T(1-\sin^2 heta_T\cos^2\phi_T) \ imes \ \mathcal{T}_+ \ &+ ig|A_{\parallel}ig|^2 \ \sin^2\psi_T(1-\sin^2 heta_T\sin^2\phi_T) \ imes \ \mathcal{T}_+ \ &+ ig|A_{\perp}ig|^2 \ \sin^2\psi_T\sin^2 heta_T \ imes \ \mathcal{T}_- \ &- ig|A_{\parallel}ig|A_{\perp}ig|\sin^2\psi_T\sin(2 heta_T)\sin\phi_T \ imes \ \mathcal{U} \ &+ ig|A_{\parallel}ig|A_0ig|\cos\delta_{\parallel}igg(rac{1}{\sqrt{2}}ig)\sin(2\psi_T)\sin^2 heta_T\sin(2\phi_T) \ imes \ \mathcal{T}_+ \ &+ ig|A_{\perp}ig|A_0igg|\cos\delta_{\parallel}igg(rac{1}{\sqrt{2}}igg)\sin(2\psi_T)\sin^2 heta_T\sin(2\phi_T) \ imes \ \mathcal{T}_+ \end{aligned}$$

$$\begin{split} \mathcal{T}_{+} &= e^{-\Gamma t} \times \left[\cosh(\Delta\Gamma t/2) - \cos(2\beta_{s}) \sinh(\Delta\Gamma t/2) \mp \sin(2\beta_{s}) \sin(\Delta m_{s}t) \right] \\ \mathcal{T}_{-} &= e^{-\Gamma t} \times \left[\cosh(\Delta\Gamma t/2) + \cos(2\beta_{s}) \sinh(\Delta\Gamma t/2) \pm \sin(2\beta_{s}) \sin(\Delta m_{s}t) \right] \\ \mathcal{U} &= \pm e^{-\Gamma t} \times \left[\sin(\delta_{\perp} - \delta_{\parallel}) \cos(\Delta m_{s}t) - \cos(\delta_{\perp} - \delta_{\parallel}) \cos(2\beta_{s}) \sin(\Delta m_{s}t) \right] \\ &\pm \cos(\delta_{\perp} - \delta_{\parallel}) \sin(2\beta_{s}) \sinh(\Delta\Gamma_{s}t/2) \right] \\ \mathcal{V} &= \pm e^{-\Gamma t} \times \left[\sin\delta_{\perp} \cos(\Delta m_{s}t) - \cos\delta_{\perp} \cos(2\beta_{s}) \sin(\Delta m_{s}t) \right] \\ &\pm \cos(\delta_{\perp}) \sin(2\beta_{s}) \sinh(\Delta\Gamma_{s}t/2) \right] \end{split}$$

changes for B⁰/B⁰ tags

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Result of fit: (FPCP 2010, 5.2 fb⁻¹)







Nicely consistent with SM! (0.8-1.0 σ)

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- $\operatorname{Iavi} A$ Belle has also studied B_s decays with Y(5S) data



$$N = (129 \text{ fb}^{-1}) \times (0.302 \text{ nb}) \times (0.193) \times 2 = \begin{bmatrix} 15 \times 10^6 & B_s \text{ decays} \\ \uparrow & \uparrow & \uparrow \\ Belle \text{ sample } \sigma[e^+e^- \rightarrow Y(5S)] & \mathcal{B}[Y(5S) \rightarrow B_s(^*)B_s(^*)] \end{bmatrix}$$

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| $\Upsilon(5S) \rightarrow D_s^+ X, D^0 X$ (inclusive) $J/\psi X$ (inclusive) | 1.86 fb ⁻¹ | Drutskoy et al., PRL 98, 052001 (2007) |
|--|------------------------------|--|
| $B_s \rightarrow D_s^{(*)} \pi^+, D_s^{(*)} \rho^+$ $J/\psi \phi, J/\psi \eta$ | 1.86 fb ⁻¹ | Drutskoy et al., PRD 76, 012002 (2007) |
| $B_s \rightarrow \phi \gamma, \gamma \gamma$ (upper limit) | 23.6 fb ⁻¹ | Wicht et al., PRL 100, 121801 (2008) |
| $Y(5S) \rightarrow Y(1S)\pi^{+}\pi, Y(1S)K^{+}K^{-},$ $Y(2S)\pi^{+}\pi, Y(3S)\pi^{+}\pi^{-}$ | 21.7 fb ⁻¹ | Chen et al., PRL 100, 112001 (2008) |
| $B_s \rightarrow D_s \pi^+, D_s K^+$ | 23.6 fb ⁻¹ | Louvot et al., PRL 102, 021801 (2009) |
| $B_s ightarrow D_s^* \pi^+, \ D_s^{(*)} ho^+$ (with polarization) | 23.6 fb ⁻¹ | Louvot (EPF-Lausanne), submitted to PRD |
| $B_s \longrightarrow K^+K^-$, K_SK_S , $K^-\pi^+$, $\pi^+\pi^-$ | 23.6 fb ⁻¹ | Peng (NTU-Taiwan), ~submitted to PRL |
| $B_s \rightarrow J/\psi\eta, J/\psi\eta'$ | 23.6 fb ⁻¹ | Li (Hawaii), presented at BEAUTY'09 |
| $B_s \rightarrow D_s^{(*)} D_s^{(*)}$ | 23.6 fb ⁻¹ | Esen (Cincinnati), submitted to PRL |
| $Y(5S) \rightarrow Y(1S)\pi^{+}\pi, Y(2/3S)\pi^{+}\pi$ | 8.2 fb ⁻¹ | Chen (NTU-Taiwan), presented at ICHEP'08 |
| $\Upsilon(5S) \rightarrow BB\pi, BB\pi\pi$ | 23.6 fb ⁻¹ | Drutskoy (Cincinnati), submitted to PRD |

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Esen, Schwartz et al. (Belle), arXiv:1005.5177, submitted to PRL [23 fb⁻¹]

The partial width of (Cabibbo-favored) $B_s \rightarrow D_s^{*+}D_s^{*-}$ is expected to dominate the decay width difference between B_s - B_s mass eigenstates. Aleksan et al., PLB 316, 567 (1993)

⇒ Measuring the branching fraction constrains $\Delta\Gamma_s/\Gamma_s$, which is an important mixing parameter in the B_s system. Our results are competitive with CDF/D0.

23.6 fb⁻¹: We reconstruct $D_s^{*+} \rightarrow D_s^{+} \gamma$. To maximize sensitivity, reconstruct 6 D_s final states: $\phi \pi^+, K^{*0} K^+, K_s K^+, \phi \rho^+, K_s K^{*+}, K^{*0} K^{*+}$



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Two-dimensional fit for event yields:



$$\mathcal{B} = (6.9 \pm 1.5 \pm 1.9)\%$$
$$\Delta \Gamma_s / \Gamma_s = 2\mathcal{B} / (1 - \mathcal{B})$$

 $N_{signal} = 22.5 + 4.7 - 3.9$

$$= 0.147 + 0.04 \pm 0.04$$

Compare to 2010 PDG: $\Delta \Gamma_{\rm s} / \Gamma_{\rm s} = 0.092 \, {}^{+0.051}_{-0.054}$

aviA The Future: KEKB+Belle -> SuperKEKB+Belle II

Why do this? Why is a flavor factory so important?

- A flavor factory studies processes that occur at 1-loop in the SM but may be O(1) in NP: FCNC, neutral meson mixing, CP violation. These loops probe energy scales that cannot be accessed directly (even at the LHC).
- Current experimental bounds NP scale is 10-100 TeV; thus, if the LHC finds NP at O(1) TeV, it must have a nontrivial flavor/phase structure
- Even if no new sources of CPV or flavor violation, current SM couplings are sufficient to provide sensitivity to new particles at a super flavor factory
- SM CP violation is insufficient to account for baryogenesis of matterdominated universe; must be other sources of CPV
- If supersymmetry is found at the LHC, a crucial question will be: how is it broken. By studying flavor couplings, a flavor factory can address this.

A (super) flavor factory searches for NP by phases, CP asymmetries, inclusive decay processes, rare leptonic decays, absolute branching fractions. There is a wide range of observables. These are <u>complementary</u> to the LHC Atlas and CMS experiments, which will search for NP via direct new particle production at high- p_{T} .

Project was just approved! http://kek.jp/intra-e/press/2010/KEKBupgrade.html

$FlaviA KEKB \rightarrow SuperKEKB (nano-beam)$







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3 year shut-down for upgrade of the accelerator and detector
Start machine operation in 2014





$$egin{array}{rcl} {\cal A}_t &=& |A_t| \, e^{i \phi_t} \, e^{i \delta_t} \ {\cal A}_p &=& |A_p| \, e^{i \phi_p} \, e^{i \delta_p} \end{array}$$

$$\begin{split} \Gamma(B \to f) &= |\mathcal{A}_t + \mathcal{A}_p|^2 \\ &= |A_t|^2 + |A_p|^2 + 4|A_t||A_p|\cos(\Delta\phi + \Delta\delta), \end{split}$$

$$\begin{pmatrix} \Delta \phi &= \phi_t - \phi_p \ \Delta \delta &= \delta_t - \delta_p \end{pmatrix}$$

$$egin{array}{rcl} ar{\mathcal{A}}_t &=& |A_t| \, e^{-i \phi_t} \, e^{i \delta_t} \ ar{\mathcal{A}}_p &=& |A_p| \, e^{-i \phi_p} \, e^{i \delta_p} \end{array}$$

$$\begin{split} \Gamma(\bar{B} \to \bar{f}) &= \left| \bar{\mathcal{A}}_t + \bar{\mathcal{A}}_p \right|^2 \\ &= \left| A_t \right|^2 + \left| A_p \right|^2 + 4 |A_t| |A_p| \cos(-\Delta \phi + \Delta \delta), \end{split}$$

$$\Rightarrow \ \ \, A_{CP} \ \equiv \ \frac{\Gamma(\bar{B} \to \bar{f}) - \Gamma(B \to f)}{\Gamma(\bar{B} \to \bar{f}) + \Gamma(B \to f)} \ \propto \ \sin \Delta \phi \ \sin \Delta \delta$$

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$$A_{CP} \;\equiv\; rac{\Gamma(ar{B}
ightarrow ar{f}) - \Gamma(B
ightarrow f)}{\Gamma(ar{B}
ightarrow ar{f}) + \Gamma(B
ightarrow f)} \;\propto\; \sin\Delta\phi\,\sin\Delta\delta$$



diagrams identical except for "spectator" quark \Rightarrow strong and weak phases are the same, A_{CP} should be the same...

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$\mathbf{F}_{net} \overset{\text{Iavi}}{\mathsf{A}} Measuring direct CPV with B \rightarrow K\pi$

But they are not (?!) (Belle, Nature 452, p332, 2008):



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FlaviA Measuring direct CPV at Belle

``Model independent'' sum rule for all four modes: Gronau, PLB 627, 82 (2005); Atwood & Soni, PRD 58, 036005 (1998):

$$\mathcal{A}_{CP}(K^{+}\pi^{-}) + \mathcal{A}_{CP}(K^{0}\pi^{+})\frac{\mathcal{B}(K^{0}\pi^{+})}{\mathcal{B}(K^{+}\pi^{-})}\frac{\tau_{0}}{\tau_{+}} = \mathcal{A}_{CP}(K^{+}\pi^{0})\frac{2\mathcal{B}(K^{+}\pi^{0})}{\mathcal{B}(K^{+}\pi^{-})}\frac{\tau_{0}}{\tau_{+}} + \mathcal{A}_{CP}(K^{0}\pi^{0})\frac{2\mathcal{B}(K^{0}\pi^{0})}{\mathcal{B}(K^{+}\pi^{-})}$$



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$$\mathcal{A}_{CP}(K^{+}\pi^{-}) + \mathcal{A}_{CP}(K^{0}\pi^{+})\frac{\mathcal{B}(K^{0}\pi^{+})}{\mathcal{B}(K^{+}\pi^{-})}\frac{\tau_{0}}{\tau_{+}} = \mathcal{A}_{CP}(K^{+}\pi^{0})\frac{2\mathcal{B}(K^{+}\pi^{0})}{\mathcal{B}(K^{+}\pi^{-})}\frac{\tau_{0}}{\tau_{+}} + \mathcal{A}_{CP}(K^{0}\pi^{0})\frac{2\mathcal{B}(K^{0}\pi^{0})}{\mathcal{B}(K^{+}\pi^{-})}\frac{2\mathcal{B}(K^{0}\pi^{0})}{\mathcal{B}(K^{+}\pi^{-})}\frac{2\mathcal{B}(K^{0}\pi^{0})}{\mathcal{B}(K^{+}\pi^{-})}\frac{2\mathcal{B}(K^{0}\pi^{0})}{\mathcal{B}(K^{+}\pi^{-})}\frac{2\mathcal{B}(K^{0}\pi^{0})}{\mathcal{B}(K^{+}\pi^{-})}\frac{2\mathcal{B}(K^{0}\pi^{0})}{\mathcal{B}(K^{0}\pi^{0})}\frac{2\mathcal{B}(K^{0}\pi^{0})}\mathcal{B}(K^{0}\pi^{0})}\frac{2\mathcal{B}(K^{0}\pi^{0})}{\mathcal{B}(K^{0}\pi^{0})}\frac{2\mathcal{B}(K^{0}\pi^{0})}\mathcal{B}(K^{0}\pi^{0})}\frac{2\mathcal{B}(K^{0}\pi^{0})}\mathcal{B}(K^{0}\pi^{0})}\frac{2\mathcal{B}(K^{0}\pi^{0})}{\mathcal{B}(K^{0}\pi^{0})}\frac{2\mathcal{B}(K^{0}\pi^{0})}\mathcal{B}(K^{0}\pi^{0})}\frac{2\mathcal{B}(K^{0}\pi^{0})}\mathcal{B}(K^{0}\pi^{0})}\frac{2\mathcal{B}(K^{0}\pi^{0})}\mathcal{B}(K^{0}\pi^{0})}\frac{2\mathcal{B}(K^{0}\pi^{0})}\mathcal{B}(K^{0}\pi^{0})}\frac{2\mathcal{B}(K^{0}\pi^{0})}\mathcal{B}(K^{0$$

B factory at 50 fb⁻¹, with today's central values:



FlaviA Summary of Belle II/Super-B (Italy)



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